Adaptive Harmonic Spectral Decomposition for Multiple Pitch Estimation

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Abstract-Multiple pitch estimation consists of estimating the fundamental frequencies and saliences of pitched sounds over short time frames of an audio signal. This task forms the basis of several applications in the particular context of musical audio. One approach is to decompose the short-term magnitude spectrum of the signal into a sum of basis spectra representing individual pitches scaled by time-varying amplitudes, using algorithms such as nonnegative matrix factorization (NMF). Prior training of the basis spectra is often infeasible due to the wide range of possible musical instruments. Appropriate spectra must then be adaptively estimated from the data, which may result in limited performance due to overfitting issues. In this paper, we model each basis spectrum as a weighted sum of narrowband spectra representing a few adjacent harmonic partials, thus enforcing harmonicity and spectral smoothness while adapting the spectral envelope to each instrument. We derive a NMF-like algorithm to estimate the model parameters and evaluate it on a database of piano recordings, considering several choices for the narrowband spectra. The proposed algorithm performs similarly to supervised NMF using pre-trained piano spectra but improves pitch estimation performance by 6% to 10% compared to alternative unsupervised NMF algorithms.

Index Terms—Adaptive representation, harmonicity, multiple pitch estimation, nonnegative matrix factorization, spectral smoothness.

I. INTRODUCTION

W USIC signals involve a collection of sounds, which may be either pitched or unpitched. Multiple pitch estimation consists of estimating the fundamental frequencies of pitched sounds within short time frames and quantifying confidence in these estimates by means of a salience measure [1]. The resulting mid-level representation can be exploited as a front-end for several music information retrieval and signal processing applications. For instance, automatic music transcription is usually achieved by tracking frame-by-frame pitch estimates over time so as to select musical notes with high salience and find their onset time, duration, pitch, and voice [2]. Multiple pitch estimation has also been used for chord detection [3], instrument identification [4], and source separation [5].

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A variety of approaches have been proposed to address multiple pitch estimation in the literature [1], ranging from correlograms [6], spectral peak clustering [7], and harmonic sum [8] to probabilistic models [9]-[11], neural networks [12], and support vector machines [13]. One particular approach is to decompose the short-term magnitude or power spectrum of the signal into a sum of basis spectra representing individual pitches scaled by time-varying amplitudes. The basis spectra can be either fixed by training on annotated recordings [14]-[16] or adaptively estimated from the observed spectra [17]-[21]. The parameters of this model can be estimated by nonnegative matrix factorization (NMF), sparse decomposition, or sparse dictionary learning. These algorithms minimize distortion between observed and model spectra, given some optional temporal priors such as continuity and sparsity. Fixed basis spectra typically achieve better performance, provided that test and training data involve the same instruments in similar recording conditions, which is difficult to satisfy in practice. Adaptive basis spectra address this issue, but result in limited performance due to the lack of constraints ensuring that each basis spectrum has a clearly identifiable pitch. Constraints of spectral shift invariance [22] or source-filter modeling [23] favor more structured spectra. However, they do not guarantee that the estimated spectra are harmonic. Experiments in [24] suggest that these constraints are respectively inappropriate and insufficient: shift invariance does not account for variations of spectral envelope as a function of pitch, while source-filter modeling includes a large number of parameters that are difficult to estimate reliably.

A more principled approach to the estimation of adaptive pitched basis spectra is to design explicit harmonicity constraints. In [25], each basis spectrum is constrained to zero in all bins but the multiples of a fixed fundamental frequency. This model relies on a crude approximation of the spectrum of a sinusoidal partial and is prone to errors since the harmonicity constraint alone does not allow segregation between a given fundamental frequency and its submultiples. In [26] and [24], each basis spectrum is modeled as a weighted sum of spectra representing individual partials and the weights are constrained via a source-filter model, where the source weights are either trained specifically for singing voice [26] or estimated from the test data [24]. This additional constraint appears efficient in the context of melody transcription or source separation, provided each instrument plays a sufficient number of different pitches and its observed pitch range is known [24]. In [27] and [28], we introduced a different approach whereby each basis spectrum is modeled as a weighted sum of narrowband spectra with a smooth envelope representing a few adjacent harmonic partials. This approach reduces octave errors without assuming prior dependencies between the spectral envelopes of different pitches. It is

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perhaps closer to low-level auditory processing of pitch, which relies on the presence of several partials within certain auditory bands [1]. Inharmonicity and variable tuning constraints were also explored in [28] but did not bring any improvement.

In this paper, we further investigate the use of harmonicity and spectral smoothness as explicit constraints for NMF-based adaptive spectral decomposition, independently of any temporal prior. We extend our preliminary work in several ways. First, we study several definitions for the narrowband spectra, including training from annotated recordings. Second, we consider a range of distortion measures. Third, we evaluate our algorithm on a more diverse database, compare it to the alternative approaches discussed above, and quantify its robustness to the chosen parameter values. The structure of the rest of the paper is as follows. In Section II, we describe baseline NMF-based algorithms and provide example results. We present the proposed adaptive harmonic model and the associated algorithm in Section III. We evaluate these algorithms on a database of music recordings in Section IV and conclude in Section V.

II. BASELINE DECOMPOSITIONS OVER FIXED OR UNCONSTRAINED BASIS SPECTRA

Baseline NMF-based algorithms for multiple pitch estimation involve the following steps: computing a time–frequency representation of the signal, decomposing it into a scaled sum of fixed or adaptive basis spectra, identifying the pitch of each spectrum in the latter case, and deriving a pitch salience measure from the associated time-varying amplitudes. Each of these steps involves some design choices outlined below.

A. ERB-Scale Time–Frequency Representation

In order to discriminate musical pitches, the time-frequency representation must have a resolution of at least one semitone over the whole frequency range. This can be achieved using the short-time Fourier transform (STFT) with a long window [19], a constant-Q filterbank [22], or another nonuniform filterbank. In the following, we consider the auditory-motivated filterbank in [15]. The input signal is passed through a set of F = 250 filters indexed by f consisting of sinusoidally modulated Hann windows with frequencies ν_f linearly spaced between 5 Hz and 10.8 kHz on the Equivalent Rectangular Bandwidth (ERB) scale [29] given by $\nu_f^{\text{ERB}} = 9.26 \log(0.00437 \nu_f^{\text{Hz}} + 1)$. The length L_f of each filter is set so that the bandwidth of its main frequency lobe equals four times the difference between its frequency and those of adjacent filters. Each subband is then partitioned into disjoint 23-ms time frames indexed by t and the root-mean-square magnitude X_{ft} is computed within each frame. This yields similar pitch estimation performance to the STFT at a lower computation cost due to reduction of the number of frequency bins [27].

B. Magnitude-Domain NMF With β -Divergence

NMF refers to a set of algorithms minimizing some distortion measure between the observed spectrum X_{ft} and the model spectrum Y_{ft} defined as

$$Y_{ft} = \sum_{i=1}^{I} A_{it} S_{if} \tag{1}$$

where S_{if} and A_{it} , $i \in \{1, \ldots, I\}$, are a set of basis spectra and time-varying amplitudes, respectively. This model has been applied to magnitude spectra [17] or, more rarely, power spectra [15]. Different parametric distortion measures have been employed within the family of β -divergences [30]

$$d(X_{ft}|Y_{ft}) = \frac{1}{\beta(\beta-1)} \left(X_{ft}^{\beta} + (\beta-1)Y_{ft}^{\beta} - \beta X_{ft}Y_{ft}^{\beta-1} \right)$$
(2)

including the Euclidean distance ($\beta = 2$) [17], Kullback-Leibler divergence ($\beta \rightarrow 1$) [17] and Itakura-Saito divergence ($\beta \rightarrow 0$) [18], or within the family of perceptually weighted Euclidean distances [27]. Both families involve a parameter $\beta \geq 0$ that can be chosen so that the distortion scales with X_{ft}^{β} . A small β compresses the large dynamic range of music, hence increasing the modeling accuracy of quiet sounds. In the following, we use magnitude spectra and measure distortion via β -divergence.

The model parameters can be estimated either by inferring both adaptive basis spectra and time-varying amplitudes from the test data or by learning fixed basis spectra from training data and inferring their time-varying amplitudes only from the test data. Training and inference are both achieved by minimization of the chosen distortion measure. After suitable initialization of the parameters, the β -divergence can be minimized by iterative application of one or both of the following multiplicative updates rules until convergence [30]

$$A_{it} \leftarrow A_{it} \frac{\sum_{f=1}^{F} S_{if} Y_{ft}^{\beta-2} X_{ft}}{\sum_{f=1}^{F} S_{if} Y_{ft}^{\beta-1}}$$
(3)

$$S_{if} \leftarrow S_{if} \frac{\sum_{t=1}^{T} A_{it} Y_{ft}^{\beta - 2} X_{ft}}{\sum_{t=1}^{T} A_{it} Y_{ft}^{\beta - 1}}.$$
 (4)

Initialization is achieved either by randomly drawing A_{it} and S_{if} from a uniform distribution when estimating the spectra or by setting A_{it} to 1 when considering fixed spectra. Although it has been proved that β -divergence is nonincreasing under these updates for $1 \le \beta \le 2$ only [31], experimental convergence has been observed for any β [30], [21].

C. Harmonic Comb-Based Pitch Identification

We measure the pitch p_i of a given basis spectrum S_{if} on the Musical Instrument Digital Interface (MIDI) semitone scale related to its fundamental frequency ν_{i0}^{Hz} via

$$\nu_{i0}^{\text{Hz}} = 440 \times 2^{\frac{p_i - 69}{12}}.$$
(5)

When training the basis spectra on annotated data, each basis spectrum is associated *a priori* with a fixed integer pitch and accurate training is ensured by setting to zero the amplitudes of the basis spectra corresponding to inactive pitches. By contrast, basis spectra estimated from the test data may be either pitched or unpitched and their pitches must be found *a posteriori*. In the following, we use the sinusoidal comb estimator [27]

$$\nu_{i0}^{\rm Hz} = \arg\min_{\nu_0^{\rm Hz}} \sum_{f=1}^F S_{if}^2 \left[1 - \cos\left(2\pi\nu_f^{\rm Hz}/\nu_0^{\rm Hz}\right) \right].$$
(6)

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Fig. 1. Comparison of several NMF-based algorithms for multiple pitch estimation of the first 30 s of Borodin's *Little Suite—Serenade* for piano. Top row: magnitude spectrum and ground-truth pitch activity. Second row: basis spectra estimated via unconstrained NMF, sorted in order of increasing pitch, and resulting pitch activity. Third row: basis spectra trained on the MIS database and resulting pitch activity. Bottom row: basis spectra estimated via NMF under harmonicity and spectral smoothness constraints (implemented with gammatone windows of order n = 4, b = 11/3 ERB, $K_{max} = 6$) and resulting pitch activity. In the three lower rows, the estimated active pitches are indicated in black over the ground truth pitches in gray.

The pitch range is chosen as the interval between $p_{\rm low} = 21$ (27.5 Hz) and $p_{\rm high} = 108$ (4.19 kHz), which is the range of the piano. The basis spectra whose estimated pitch is outside this range are classified as unpitched. We found that, despite its simplicity, this estimator was surprisingly efficient for the post-processing of basis spectra estimated via NMF, whose characteristics differ significantly from those of clean musical instrument notes.

D. Amplitude-Based Pitch Salience Measure

Given the time-varying amplitudes of all basis spectra, we measure the salience of an integer pitch p by the square root of the total power of the scaled basis spectra whose pitch p_i is within one quarter-tone of p

$$\bar{A}_{pt} = \left(\sum_{f=1}^{F} \left(\sum_{i \text{ s.t. } |p_i - p| < 1/2} A_{it} S_{if}\right)^2\right)^{1/2}.$$
 (7)

This measure scales as an amplitude and is hence comparable to other amplitude-based measures, such as the harmonic sum in [8]. Due to their real-valued output, such measures cannot be directly compared to ground truth annotations which characterize a given pitch as either active or inactive. Instead, we derive pitch estimates on a frame-by-frame basis by classifying a given pitch p as active whenever

$$\bar{A}_{pt} \ge 10^{A_{\min}/20} \max_{pt} \bar{A}_{pt} \tag{8}$$

where A_{\min} is a detection threshold in decibels (dB) that can be either set manually or learned from training data. We found that this decision strategy was more efficient than the one in [8] for the estimation of the number of active pitches per frame.

E. Example Results

The second and third rows of Fig. 1 illustrate the multiple pitch estimation results derived from NMF with adaptive or fixed basis spectra over an excerpt of Borodin's *Little Suite—Serenade*, recorded from an acoustic piano and taken from the MIDI-Aligned Piano Sounds (MAPS) database [32]. The number of basis spectra was set to $I = p_{high}-p_{low}+1 = 88$

and β was set to its optimal value determined in Section IV. Training was conducted on the University of Iowa's musical instrument samples (MIS) [33], which include isolated note sounds from a single piano at all pitches and at three loudness levels. The detection threshold A_{\min} was set to -25 dB.

We observe that many basis spectra estimated via adaptive NMF are neither clearly pitched nor unpitched. Most spectra involve spurious spectral peaks besides the predominant harmonic series or missing peaks in that series. Some spectra even represent several pitches at a time. The resulting pitch activity representation exhibits short-duration errors that could be easily addressed in a postprocessing stage involving a temporal model, but also longer-duration errors, such as pitches below or above the restricted pitch range of the excerpt, that would be less easily handled. The pitch activity representation estimated from the fixed spectra involves even more errors. Although the trained basis spectra are clearly pitched, their spectral envelopes do not match those of the piano spectra in the test excerpt. Several pitches at integer fundamental frequency ratios are then combined to represent a single note.

III. ADAPTIVE HARMONIC DECOMPOSITION

In order to avoid the above pitch estimation errors, it appears sensible to constrain each basis spectrum to represent a single note but to adapt its spectral envelope to the test data. We achieve these goals by adding constraints over the fine structure of the basis spectra within the model, but leaving some degrees of freedom over their spectral envelope.

A. General Framework for Spectral Fine Structure Constraints

We associate each basis spectrum S_{if} with an integer pitch p and index by $j \in \{1, \ldots, J_p\}$ the basis spectra having the same pitch but different spectral envelopes. The model spectrum (1) is then equivalently written as

$$Y_{ft} = \sum_{p=p_{\text{low}}}^{p_{\text{high}}} \sum_{j=1}^{J_p} A_{pjt} S_{pjf}.$$
(9)

In order to ensure that each spectrum S_{pjf} actually models the expected pitch p, we constrain it as

$$S_{pjf} = \sum_{k=1}^{K_p} E_{pjk} N_{pkf} \tag{10}$$

where N_{pkf} , $k \in \{1, \ldots, K_p\}$ are fixed narrowband spectra enforcing the spectral fine structure associated with that pitch and the coefficients E_{pjk} parametrize the spectral envelope. The estimation of the model parameters now consists of inferring the spectral envelope and the time-varying amplitude of each basis spectrum from the test data, given its prior fine structure. Due to the linearity of constraint (10), the estimation of each of these two quantities can be recast into the standard NMF framework. The β -divergence can be minimized using the following multiplicative updates rules

$$A_{pjt} \leftarrow A_{pjt} \frac{\sum_{f=1}^{F} S_{pjf} Y_{ft}^{\beta-2} X_{ft}}{\sum_{f=1}^{F} S_{pjf} Y_{ft}^{\beta-1}}$$
(11)

$$E_{pjk} \leftarrow E_{pjk} \frac{\sum_{f=1}^{F} \sum_{t=1}^{T} A_{pjt} N_{pkf} Y_{ft}^{\beta-2} X_{ft}}{\sum_{f=1}^{F} \sum_{t=1}^{T} A_{pjt} N_{pkf} Y_{ft}^{\beta-1}} \quad (12)$$

whose convergence can be proved under the same conditions as above. In the following, we initialize the parameters prior to application of these rules by setting A_{pjt} to 1 and choosing E_{pjk} so that the basis spectra have a constant initial slope of $-6 \times j$ dB/octave over the whole frequency range regardless of their pitch.

B. Harmonicity and Spectral Smoothness Constraints

The constraint (10) can represent a range of spectral fine structures associated with different instrument classes, including, e.g., harmonic partials for woodwinds, slightly inharmonic partials for plucked strings, or very inharmonic partials for bells. Given the frequencies of the partials, each fine structure spectrum N_{pkf} can be defined as a weighted sum of the spectra of individual partials

$$N_{pkf} = \sum_{m=1}^{M_p} W_{pkm} P_{pmf} \tag{13}$$

where P_{pmf} is the magnitude spectrum of the *m*th overtone partial, M_p is the number of partials, and the weights W_{pkm} parametrize the spectral shape of band k.

The spectrum of each partial can be analytically derived from the frequency responses of the bandpass filters associated with the frequency bins of the time–frequency transform. For the filterbank in Section II-A, we get

$$P_{pmf} = \left| \operatorname{sinc} \left[L_f \left(\nu_f^{\mathrm{Hz}} - \nu_{pm}^{\mathrm{Hz}} \right) \right] + \frac{1}{2} \operatorname{sinc} \left[L_f \left(\nu_f^{\mathrm{Hz}} - \nu_{pm}^{\mathrm{Hz}} \right) + 1 \right] + \frac{1}{2} \operatorname{sinc} \left[L_f \left(\nu_f^{\mathrm{Hz}} - \nu_{pm}^{\mathrm{Hz}} \right) - 1 \right] \right|$$
(14)

where ν_{pm}^{Hz} is the frequency of the *m*th partial in Hz, sinc is the sine cardinal function, and L_f is the length in seconds of the filter associated with bin *f*. We previously showed that the modeling of inharmonicity or variable tuning in this context does not significantly affect multiple pitch transcription performance on piano data compared to a harmonic model with fixed tuning [28]. Therefore, we assume that the frequencies of the partials follow the exact harmonic model

$$\nu_{pm}^{\rm Hz} = m \, \nu_{p0}^{\rm Hz} \tag{15}$$

where the fundamental ν_{p0}^{Hz} corresponding to pitch p is defined in (5). All harmonics may be observed, hence the number of partials is set to $M_p = \lfloor \nu_F^{\text{Hz}} / \nu_{p0}^{\text{Hz}} \rfloor$ where $\lfloor \cdot \rfloor$ denotes the floor function and ν_F^{Hz} the frequency of the topmost frequency bin.

The choice of the weights W_{pkm} in (13) affects pitch estimation performance. When each fine structure spectrum N_{pkf} represents a single partial, the basis spectra S_{pjf} may encode multiples of the expected fundamental frequency, resulting in substitution errors. When it contains too many partials, the basis

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spectra may not adapt well to the spectral envelope of the instruments, leading to insertion or deletion errors. In order to avoid such errors, each fine structure spectrum should span a narrow frequency band containing a few partials. The relative amplitudes of these partials may be chosen under the additional constraint of spectral smoothness, exploited by some other pitch estimation algorithms [8], enforcing similar amplitudes for adjacent partials. Practical implementations of this constraint typically rely either on the properties of auditory pitch perception or those of musical instrument sounds.

We investigate a range of implementations by exploring different choices for the center frequencies, the bandwidths and the shapes of the fine structure spectra. The weights W_{pkm} are defined as

$$W_{pkm} = w \left(\frac{\nu_{pm} - \nu_{p0} - (k-1)b}{2b} \right)$$
(16)

where w is a chosen window function, ν_{p0} and ν_{pm} denote the frequency of the fundamental and that of the *m*th partial on a chosen frequency scale, *b* is the spacing between successive frequency bands, and 2b their bandwidth on that scale. The shape of the frequency bands is governed by w and their center frequencies are uniformly spaced on the chosen frequency scale, starting from the fundamental. The choice of a larger bandwidth 2b than the minimum bandwidth *b* needed for full coverage increases the smoothness of the resulting basis spectra. Similarly to the above, all frequency bands are assumed to be observed up to a maximum index K_{max} so that the number of frequency bands is set to $K_p = \min(\lfloor(\nu_F - \nu_{p0})/b\rfloor + 1, K_{\text{max}})$ with ν_F the frequency of the topmost frequency bin expressed on the chosen scale. The maximum total bandwidth is then equal to $b_{\text{max}} = K_{\text{max}} b$.

In the following, we consider three particular frequency scales: the pitch-synchronous linear scale indicating the partial index

$$\nu^{\text{psyn}} = \frac{\nu^{\text{Hz}}}{\nu_{n0}^{\text{Hz}}} \tag{17}$$

the logarithmic octave scale

$$\nu^{\rm oct} = \log_2 \nu^{\rm Hz} \tag{18}$$

and the ERB scale

$$\nu^{\text{ERB}} = 9.26 \log(0.00437\nu^{\text{Hz}} + 1). \tag{19}$$

In parallel, we consider four symmetric window functions of unitary bandwidth: the rectangular window

$$w^{\text{rect}}(u) = \begin{cases} 1, & \text{if } -\frac{1}{2} \le u \le \frac{1}{2} \\ 0, & \text{otherwise} \end{cases}$$
(20)

the triangular window

$$w^{\text{triang}}(u) = \begin{cases} 1 - |u|, & \text{if } -1 \le u \le 1\\ 0, & \text{otherwise} \end{cases}$$
(21)



Fig. 2. Basis spectrum S_{pjf} estimated for the piano excerpt in Fig. 1 given fixed harmonic fine structure spectra N_{pkf} (p = 60, gammatone windows of order n = 4, b = 11/3 ERB, $K_{max} = 6$).

the Hann window

$$w^{\text{hann}}(u) = \begin{cases} \frac{1}{2}(1 + \cos \pi u), & \text{if } -1 \le u \le 1\\ 0, & \text{otherwise} \end{cases}$$
(22)

and the "gammatone" window of order n [34]

$$w^{\text{gamma}}(u) = \frac{1}{(1+k^2u^2)^n} \text{ with}$$
$$k = \frac{\sqrt{\pi}\Gamma(n-1/2)}{\Gamma(n)}$$
(23)

with $\Gamma(\cdot)$ denoting the gamma function. By contrast with other windows, the latter has infinite support and allows control of the roll-off slope via its parameter n.

The ERB scale and the gammatone window are both perceptually motivated [34]. The spectral envelope coefficients E_{pjk} corresponding to these choices are hence closely related to the frequency-warped cepstral coefficients routinely used as timbre features for audio classification [35]. Example spectra corresponding to these choices are shown in Fig. 2. Although audiological measurements suggest that the shape of auditory bands is

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asymmetric on the ERB scale, we observed that the use of symmetric windows did not significantly affect pitch estimation performance. A similar model involving triangular windows with a spacing and a bandwidth of 2/3 octave was employed in [36] for the estimation of the amplitudes of overlapping partials given estimated pitches.

C. Example Results

The bottom row of Fig. 1 depicts the pitch estimates obtained via NMF under harmonicity and spectral smoothness constraints on the piano excerpt considered above given a pitch activity detection threshold A_{\min} of -25 dB. Comparison with the second and third rows of that figure indicates that these estimates are more accurate than with unconstrained NMF or NMF with basis spectra trained on MIS. In particular, the number of short-duration errors is decreased and the estimated pitches lie mostly within the true pitch range of the excerpt. Some basis spectra, e.g., around p = 80, are inaccurately estimated due to the lack of observed data corresponding to these pitches. However, this does not reflect in the estimated pitches.

D. Learning the Fine Structure

An alternative approach to the definition of the fine structure spectra N_{pkf} not relying on harmonicity and spectral smoothness assumptions is to train them on annotated samples of several instruments sharing similar spectral fine structures. In order to ensure that the learned spectra exhibit a narrow bandwidth, their frequency support can be constrained similarly to above via

$$N_{pkf} = 0 \text{ if } |\nu_f - \nu_{p0} - (k-1)b| > 2b \tag{24}$$

where ν_f and ν_{p0} are the frequency of bin f and the fundamental frequency measured over one of the frequency scales in (17), (18), and (19), b is the spacing between successive frequency bands, and 2b their bandwidth on that scale. The training objective can again be recast into the standard NMF framework, leading to the multiplicative update rule

$$N_{pkf} \leftarrow N_{pkf} \frac{\sum_{j=1}^{J_p} \sum_{t=1}^{T} A_{pjt} E_{pjk} Y_{ft}^{\beta-2} X_{ft}}{\sum_{j=1}^{J_p} \sum_{t=1}^{T} A_{pjt} E_{pjk} Y_{ft}^{\beta-1}} \qquad (25)$$

to be applied alternatingly with (11) and (12). By property of multiplicative updates, the constraint (24) remains true at each iteration provided it is initially satisfied.

IV. EVALUATION

A. Algorithms and Evaluation Metrics

We evaluated the algorithms in Sections II and III on two distinct datasets: a subset of the MAPS piano database [32] and the woodwind training dataset for the Multiple Fundamental Frequency Estimation task of the Third Music Information Retrieval Evaluation eXchange¹ (MIREX 2007). Algorithms based on fixed spectra were trained on isolated piano sounds from the MIS database [33] and the RWC Musical Instrument Sound Database [37], which cover the full pitch range at three loudness levels of one and three pianos, respectively.

¹http://www.music-ir.org/mirex2007/

Two additional NMF algorithms were tested for comparison: NMF under harmonicity and source-filter constraints [24] and NMF under a single harmonicity constraint identical to that in [25] except for the improved modeling of the partial spectra in (14). The distortion measure used in the original algorithms was replaced by the more general β -divergence and optimized via multiplicative updates initialized in the same way as other NMF algorithms, i.e., with a -6 dB/octave slope for the harmonic spectra and a flat slope for the filter. Four reference multiple pitch estimation algorithms were also evaluated: the correlogram-based algorithm in [6] implemented in the MIR Toolbox 1.2.1 [38], the spectral peak clustering algorithm in [7] implemented using the optimal parameter settings therein, the harmonic sum algorithm in [8] provided by its author, and the piano-specific AR model-based algorithm in [11], also provided by its author. The SONIC automatic piano music transcription algorithm [12]² was also considered. In order to allow fair comparison regardless of the input time-frequency representation, the frame size of the algorithms in [7], [8], and [11] was set to 46 ms, which is close to the effective time resolution of the ERB filterbank at the fundamental frequency corresponding to the average observed pitch.

The algorithms in [6], [7], and [11] produced frame-by-frame pitch estimates every 10 ms. All NMF algorithms as well as the algorithm in [8] provided amplitude-based pitch salience measures, which were interpolated over a 10-ms grid and used to derive pitch estimates as explained in Section II-D. Frame-byframe pitch estimates were also derived for SONIC from the onsets and durations of the estimated musical notes.

On each 10-ms frame, each of the estimated MIDI pitches was considered to be correct if it is equal to one of the ground truth MIDI pitches. Denoting by r_t , e_t and c_t the respective number of ground truth, estimated and correct pitches on frame t, performance was quantified for each test recording in terms of recall \mathcal{R} , precision \mathcal{P} and F-measure \mathcal{F} defined as [39]

$$\mathcal{R} = \frac{\sum_{t=1}^{T} c_t}{\sum_{t=1}^{T} r_t} \tag{26}$$

$$\mathcal{P} = \frac{\sum_{t=1}^{T} c_t}{\sum_{t=1}^{T} e_t} \tag{27}$$

$$\mathcal{F} = \frac{2\mathcal{R}\mathcal{P}}{\mathcal{R} + \mathcal{P}} \tag{28}$$

and averaged over each dataset. These measures were also used within past Music Information Retrieval Evaluation eXchanges (MIREX).

B. Results on Piano Data

The first dataset consists of the initial 30 s of 50 piano pieces from the MAPS database, recorded from a Disklavier acoustic piano using either close or ambiance microphones, and having a polyphony level of 3.9 on average and 9 at most. Due to the lack of sufficient annotated data from different pianos, the optimal parameter values for each algorithm were not learned *a priori*. Instead, we considered a range of values and analyzed the impact on performance of each parameter, other parameters being

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²http://lgm.fri.uni-lj.si/sonic.html.

TABLE I Average Pitch Estimation Performance Over Piano Data Using Optimal Parameter Values for Each Algorithm

Algorithm	P (%)	\mathcal{R} (%)	\mathcal{F} (%)				
No training							
Unconstrained NMF	58.9	60.0	57.8				
NMF under harmonicity constraint	63.2	60.9	60.5				
NMF under harmonicity and source- filter constraints [24]	60.1	59.1	57.5				
NMF under harmonicity and spectral smoothness constraints	71.6	65.5	67.0				
Correlogram [6]	62.1	21.6	31.5				
Spectral peak clustering [7]	43.1	23.9	30.3				
Harmonic sum [8]	65.7	57.4	60.2				
Training on piano data							
NMF with basis spectra trained on MIS	61.2	62.1	59.6				
NMF with basis spectra trained on MIS & RWC	68.6	66.7	66.0				
NMF with fine structure spectra trained on MIS & RWC	67.2	64.9	64.2				
AR generative model [11]	68.3	42.8	51.8				
Training on piano data and note tracking							
SONIC [12]	74.5	57.6	63.6				

fixed to their optimal values. Although the optimal *a posteriori* performance figures are presumably larger than with prior parameter settings, we believe that this allows fair comparison of algorithms in terms of relative performance, as well as deeper understanding of the sensitivity to each parameter.

Preliminary experiments were conducted to validate the design choices made in Section II. The proposed harmonic combbased pitch estimator was compared to the spectral product estimator in [19] and found to improve F-measure by 10% on average when applied to unconstrained adaptive basis spectra. The chosen NMF framework based on magnitude spectra and β -divergence was also compared to NMF frameworks based on power spectra or perceptually weighted Euclidean distance. Similar results were obtained for all frameworks with adaptive basis spectra. However, with fixed spectra trained on MIS and RWC, the average F-measure decreased by 8% with power-domain modeling instead of magnitude-domain modeling and by 11% with perceptually weighted Euclidean distance instead of β -divergence.

For all NMF algorithms, various numbers of basis spectra were tested among multiples of 88, the distortion measure parameter β was varied between 0 and 2 in steps of 0.1 and the detection threshold A_{\min} between -40 and -15 dB in steps of 1 dB. For the proposed NMF algorithm, additional preliminary experiments showed that, although the effect on performance of the maximum number of frequency bands K_{\max} and their bandwidth b are related, that of K_{\max} and the maximum total bandwidth B_{\max} are roughly independent. The latter was varied in steps of 1 partial, 1/3 octave or 2 ERB, depending on the chosen frequency scale, and b was derived as $b = B_{\max}/K_{\max}$.

The results with the optimal parameter values are given in Table I. The proposed algorithm with fixed fine structure spectra resulted in an average F-measure of 67%, that is 7% to 37% better than reference multiple pitch estimation algorithms not based on NMF and 3% better than SONIC which includes temporal tracking. This level of performance is comparable to that of NMF with fixed spectra trained on both MIS and RWC, but about 9% better than unconstrained NMF, 6% better than



Fig. 3. Variation of the average pitch estimation performance over piano data as a function of the divergence parameter β and the detection threshold A_{\min} .

NMF under harmonicity constraint alone and 10% better than NMF under harmonicity and source-filter constraints. This confirms that harmonicity is an appropriate but insufficient constraint in the context of pitch estimation and suggests that spectral smoothness is more useful than source-filter modeling as an additional constraint. Fine structure spectra learned on piano data did not further improve performance compared to fixed fine structure spectra.

For all NMF algorithms, the F-measure was maximum with I = 88 basis spectra and decreased by 1 to 5% with I = 176and 2 to 7% with I = 264. Performance variation as a function of β and A_{\min} is depicted in Fig. 3. As explained in [21], a small value of β appears preferable for unconstrained NMF in order to infer wideband spectral structures despite the wide differences in dynamics between low and high frequencies. For other algorithms, the optimal β is equal to 0.5. The resulting distortion measure scales similarly to perceptual loudness for audible sounds and was also shown to be optimal in the context of audio source separation in [30]. Doubling or halving β decreases the F-measure by 0 to 5%. Unconstrained NMF also exhibits a distinct behavior from other NMF algorithms when considering the choice of A_{\min} , with an optimal value of -32 dB instead of a more conservative -27 dB. A deviation of 3 dB from the optimal A_{\min} decreases the F-measure by 1 to 2%. The harmonic sum algorithm in [8] is more sensitive to the choice of A_{\min} , with a decrease up to 7% for the same deviation.

The best results for the proposed algorithm were obtained when building fine structure spectra from gammatone windows of order n = 4 spaced on the ERB scale, with a maximum number of $K_{\text{max}} = 6$ frequency bands and a maximum total bandwidth $B_{\text{max}} = 22$ ERB. The effect of these parameters is analyzed in Tables II and III and in Fig. 4. The frequency scale has little influence, provided other parameters are adapted

TABLE II VARIATION OF THE AVERAGE PITCH ESTIMATION PERFORMANCE OVER PIANO DATA OF NMF UNDER HARMONICITY AND SPECTRAL SMOOTHNESS CONSTRAINTS FOR DIFFERENT FREQUENCY SCALES

Frequency scale	Optimal parameters	$\mathcal{F}(\%)$
	Gammatone $n = 2$	
Pitch-synchronous	$K_{\rm max} = 6$	66.1
-	$B_{\rm max} = 6$ partials	
	Gammatone $n = 4$	
Octave	$K_{\rm max} = 5$	66.5
	$B_{\rm max} = 13/3$ octaves	
	Gammatone $n = 4$	
ERB	$K_{\max} = 6$	67.0
	$B_{\rm max} = 22 \ {\rm ERB}$	

TABLE III VARIATION OF THE AVERAGE PITCH ESTIMATION PERFORMANCE OVER PIANO DATA OF NMF UNDER HARMONICITY AND SPECTRAL SMOOTHNESS CONSTRAINTS FOR DIFFERENT BAND SHAPES

Window function w	\mathcal{F} (%)
Rectangular	60.7
Triangular	64.4
Hann	63.8
Gammatone $n = 2$	66.0
Gammatone $n = 4$	67.0
Gammatone $n = 6$	66.5



Fig. 4. Variation of the average pitch estimation performance over piano data of NMF under harmonicity and spectral smoothness constraints as a function of the maximum number of frequency bands $K_{\rm max}$ and the maximum total bandwidth $B_{\rm max}$.

to the chosen scale. The bandwidth of each spectrum also has little influence, since any value of $K_{\rm max}$ between 4 and 11 or any value of $B_{\rm max}$ larger than 18 ERB results in an average F-measure within 2% of the optimum. Small values of $K_{\rm max}$ and $B_{\rm max}$ should be avoided, since they result in insufficient adaptation capabilities or incomplete coverage of the frequency axis, respectively. Finally, gammatone windows perform about 3% better than smooth windows with finite support, but the window order is not critical. Only rectangular windows should be avoided. Overall, this suggests that, even if it is not optimally

 TABLE IV

 F-MEASURE (%) FOR PITCH ESTIMATION OVER WOODWIND DATA

Algorithm	Polyphony			
Algoriuliii	2	3	4	5
Unconstrained NMF	79.9	56.3	62.1	61.9
NMF under harmonicity constraint	78.7	57.3	57.1	56.5
NMF under harmonicity and spectral smoothness constraints	76.5	64.7	67.5	62.5
Correlogram [6]	23.5	19.1	19.3	21.6
Spectral peak clustering [7]	27.8	24.7	33.5	34.0
Harmonic sum [8]	73.4	59.1	63.5	59.9

implemented, the spectral smoothness constraint still improves performance compared to the harmonicity constraint alone, provided the window w is smooth and K_{max} and B_{max} are large enough.

C. Results on Woodwind Data

Using the optimal parameter values determined in Section IV-B, we applied the algorithms not restricted to piano data to a second dataset. From the recordings of individual instrument parts of a woodwind quintet by Beethoven made available at MIREX 2007, we generated four test excerpts with two to five instruments by successively summing together the initial 30 s of the parts of flute, clarinet, bassoon, horn, and oboe. Pitch estimation results are listed in Table IV. NMF under harmonicity and spectral smoothness constraints performed best for most polyphonies, while NMF under harmonicity constraint alone sometimes performed worse than unconstrained NMF. Despite the fact that some pitches were played by up to three instruments, performance did not improve when employing more than one basis spectrum per pitch. Further experiments suggest that this is due both to the use of a constant number of basis spectra per pitch and to the difficulty of initializing these spectra so that each converges to a particular instrument.

V. CONCLUSION

We proposed an adaptive spectral decomposition model for music signals based on harmonicity and spectral smoothness constraints. This model ensures that the estimated basis spectra have a known fine structure, while their spectral envelope is adapted to the observed data. Multiple pitch estimation experiments conducted on piano and woodwind data indicate that, independently of any temporal prior, the resulting constrained NMF algorithm is potentially competitive with NMF based on fixed instrument-specific spectra and superior to unconstrained NMF or NMF under harmonicity constraint alone. As a side result, we provided a benchmark of classical NMF algorithms in the context of multiple pitch estimation and showed that the optimal value of the β -divergence parameter is often different from the integer values commonly used in the literature.

In the future, we plan to exploit the estimated amplitudebased pitch salience measure for music-to-score transcription via a probabilistic model involving additional temporal priors. Given their relationship to frequency-warped cepstral coefficients, the estimated spectral envelope coefficients could then be used to cluster the notes into instrument parts. We also aim to extend our model to represent percussive as well as pitched instruments and to improve its performance over mixtures of several instruments by using an adaptive number of basis spectra per pitch, based on recent findings regarding the estimation of the number of basis spectra [40] and their initialization [41].

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